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# Supporting to Learn Calculus Through E-test with Feedback and Self-regulation

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Abstract. This study is designed to support students in learning calculus. Many freshmen are often struggling in calculus. The reasons are many and complex; largely because the students' backgrounds are insufficient and partly because students are not involved in class, passively listening to the lectures by the traditional teaching methods. Thus, student's learning motivation is often low, and lacking of self-regulation to monitor self-learning goals. Here we intend to arouse the interest of students by technological aids, to inspire their willingness and attitude in active learning, and to train students on effective learning methods. We not only provide video materials on the campus E-teaching platform for reviews, and set up discussion forums for communication, but also offer E-test for each unit volume with feedback (see appendix) to examine students' understanding quickly. In general, several types of data including selected interviews are carefully collected and analyzed. Results in this study indicate that most students express their positive responses about these contexts to support their learning in calculus.

Keywords: E-test; Learning motivation; Scaffolding; Self-regulation

#### Introduction

In this era of educational reforms, all teachers are searching for ways to improve learning environments and instructional approaches. For example, in recent years, flipped classroom has widely challenged attention in the world, students are usually expected to watch video at home then do the exercises in the classroom and discuss the unsolved problem with classmates and teachers. Basically teacher facilitates the learning environment and provides scaffolding in cases of discussion and interaction. Under this situation, students may feel that such learning process is more funny than boring, and they certainly should have interest and motivation to achieve in these processes (Cleary & Chen, 2009).

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In the technological world, the National Council of Teachers of Mathematics (NCTM) in the United States pointed out "The curriculum should make appropriate and ongoing use of calculators and computers" (NCTM, 1989) and "Technology is essential in teaching and learning mathematics; it influences the mathematics that is taught and enhances students' learning" (NCTM, 2000). This means integrating technology in teaching and learning processes is current trend (Chen & Lai, 2015; Karadeniz, 2015; Girard, 2002; Porzio, 1995). Likewise, there is no question to extend that technology can support learning and teaching in calculus (Ben-Zvi, 2000). This study is designed for freshmen to learn calculus effectively.

Calculus is an extensive course of general mathematics. Many professional courses in high educational level need calculus as prerequisite or tool to develop further, particularly those courses provided in the college of science or engineering. Since calculus has rigorous and consistent content structures, hence learners should learn it step by step by understanding, otherwise, learners may be off the track and get lost soon. Therefore, when students learn calculus, they need to know some better ways or strategies to make progress on their goals, and teachers can advise students in these cases.

Teaching calculus engaging is really a tough endeavor, and there are no easy ways. In order to make this paper to be brief and focused, more attention is placed upon the achievement involving E-test with feedback. Note that, instead of complexity, E-test items mostly focus on big ideas in each topic and limited computation. In the whole semester, we provide eight E-tests. Besides, formal midterm and final tests generally include high level paper-and-pencil problems such as sketching graph or basic proof.

We provide appropriate learning environments with video materials and guidance, we inspire students to observe and think independently. Additionally, discussion forums and teaching assistant are lent to the learning processes of exploration, problem solving and team cooperation. Certainly, self-regulatory processes also play an important role of achievement among students (Bandura, 1986). Hopefully students can understand and apply the basic knowledge, skills, and various methods in calculus to solve problems.

#### Literature and Methods

Self-regulation refers to the ability to develop, implement, and flexibly maintain planned behavior in order to achieve one's goals. It is essential to the learning process (Jarvela & Jarvenoja, 2011; Zimmerman, 2008).

Based on teaching experience in calculus, we fully understand that students' prior knowledge and motivation may facilitate the development of self-regulation in classroom contexts. Also, research has shown that students who are able to regulate their learning in the face of the difficulties perform better than students who lack of self-regulation (Pintrich, 2000). Hence, teachers need to know influential factors and strategies to promote self-regulated learning and motivation. For instance, we tell students to see the importance in learning calculus step by step, encourage students to set attainable goals such as studying calculus together for a couple of classmates, and ask students to keep a record of the amount of time they spent on calculus every week. For each unit about calculus, we provide video materials on the campus Moodle E-teaching platform for students' reviews at any time, and set up discussion forums for communication. Moreover, we offer E-test for each unit volume with feedback (see appendix) to examine students' understanding quickly. Basically, E-test is usually open on Friday and Saturday, and students can take test at any place and any time. However, students are only given one hour to take each test, and each item is randomly presented during the test.

For convenient consideration, samples are selected from the computer science department. There are more than fifty freshmen to participate this study for one semester in calculus (II), and they are divided into two groups; Exp group and Control group; depending on the even or odd of their student identification numbers. At the beginning, please note that students in Control group have a bit higher (2 points in average) than students in Exp group regarding their background in calculus (I).

All problems in each E-test are multiple choices, please see samples in appendix. When students in Exp group provide incorrect answer in the first try, then "Hint" feedback will present immediately. At this moment, students can think about again, and they can provide next answer in the second try, and the like. When students in Control group provide incorrect answer in the first try, then there is no "Hint" feedback, but they can provide next answer in the second try based on their knowledge. On the other hand, no matter when students can employ the discussion forums to seek help or clarify their concepts. Actually, many critical data can be collected from the Moodle E-teaching platform, including their spent time in each test. Besides quantitative data, researchers also collect and analyze the interviews data from several samples.

**Procedures for E-test on line :** 



(a) Flow chart for experiment group



(b) Flow chart for control group

#### Findings and Discussions

In the whole semester, students are provided eight E-tests, each test contains 10 problems. Note that the correct ratio in the following table is calculated from the (total/10) divided by the number of students who take this E-test. For example:  $\{(197/10) / (29-4)\}=78.80\%$ . In addition, the corresponding pie chart indicates the spent time students take this test.

The firs	t E-te	est:												
Exp gr	oup	Question No.	1	2	3	4	5	6	7	8	9	10	total	Correct ratio
Total	29	Correct at first time	25	23	21	20	23	23	23	18	3	18	197	78.80%
Absent	4	Correct at second time	0	2	4	5	2	1	1	1	11	5	32	12.80%
		Third and above	0	0	0	0	0	1	1	6	11	2	21	8.40%



**Figure 1** : Outcomes of the 1<sup>st</sup> in Exp group

Control gr	oup	Question No.	1	2	3	4	5	6	7	8	9	10	total	Correct ratio
Total	29	Correct at first time	26	24	24	22	26	25	25	19	4	22	217	80.37%
Absent	2	Correct at second time	1	1	3	3	1	2	1	4	8	1	25	9.26%
		Third and above	0	2	0	2	0	0	1	4	15	4	28	10.37%



Figure 2: Outcomes of the 1st in Control group

- (1) This is the first E-test on line, students try to understand some operating environments.
- (2) At the first try, students in Control group perform a bit better.
- (3) At the second try, students in Exp group perform slightly better.
- (4) Research indicates that feedback(or hint) can assist students in improving their achievement (Nitko & Brookhart, 2010). Also, it can promote students' motivation (Wigfield, Kauda, & Cambria, 2011) and self-regulation.

The second	E-test	:
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Exp gro	up	Question No.	1	2	3	4	5	6	7	8	9	10	total	Correct ratio
Total	29	Correct at first time	12	12	10	23	17	19	20	14	16	9	152	54.29%
Absent	1	Correct at second time	6	4	7	4	6	5	4	4	3	11	54	19.29%
		Third and above	10	12	11	1	5	4	4	10	9	8	74	26.43%



Figure 3 : Outcomes of the 2<sup>nd</sup> in Exp group

Control gr	oup	Question No.	1	2	3	4	5	6	7	8	9	10	total	Correct ratio
Total	29	Correct at first time	17	13	13	21	20	22	17	12	16	15	166	61.48%
Absent	2	Correct at second time	7	8	4	1	2	2	8	5	6	6	49	18.15%
		Third and above	3	6	10	5	5	3	2	10	5	6	55	20.37%



Figure 4 : Outcomes of the 2<sup>nd</sup> in Control group

- (1) Students in Control group obviously perform better than students in Exp group do at the first try.
- (2) However, at the second try, the outcomes between two groups look very close.
- (3) It looks evident that students in Exp group generally spend longer time to take this test.

The thir	d E	-test :									
Exp grou	ιр	Question No.	1	2	3	4	5	6	7	8	9
Total	29	Correct at first time	24	10	21	19	22	20	20	24	21
Absent	1	Correct at second time	3	10	3	7	2	4	6	2	6

Third and above



1 8 4 2 4

**Figure 5** : Outcomes of the 3<sup>rd</sup> in Exp group

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Correct ratio

71.79%

17.14%

11.07%

10 total

20 201

5

2 2 1 3

4

48

31

Control g	group	Question No.	1	2	3	4	5	6	7	8	9	10	total	Correct ratio
Total	29	Correct at first time	29	10	23	20	25	22	22	22	23	20	216	74.48%
Absent	0	Correct at second time	0	12	3	6	2	5	4	4	3	3	42	14.48%
		Third and above	0	7	3	3	2	2	3	3	3	6	32	11.03%



Figure 6 : Outcomes of the 3<sup>rd</sup> in Control group

- (1) At the second try, students in Exp group perform slightly better than students in Control group do.
- (2) In case we consider the outcomes of the first try and the second try together, two groups almost make no differences.

The fou	rth E	E-test :												
Exp gro	oup	Question No.	1	2	3	4	5	6	7	8	9	10	total	Correct ratio
Total	29	Correct at first time	19	19	16	18	21	24	20	20	21	14	192	76.80%
Absent	4	Correct at second time	1	3	7	1	1	1	4	3	2	5	28	11.20%
		Third and above	5	3	2	6	3	0	1	2	2	6	30	12.00%





**Figure 7** : Outcomes of the 4<sup>th</sup> in Exp group

Control g	group	Question No.	1	2	3	4	5	6	7	8	9	10	total	Correct ratio
Total	29	Correct at first time	15	22	16	17	21	21	20	19	21	14	186	74.40%
Absent	4	Correct at second time	7	1	6	3	2	2	1	3	3	4	32	12.80%
		Third and above	3	2	3	5	2	2	4	3	1	7	32	12.80%



Figure 8 : Outcomes of the 4<sup>th</sup> in Control group

- (1) At the first try, students in Exp group perform a bit better than the students in Control group do.
- (2) No big differences between two groups exist at the second try.

Exp gro	oup	Question No.	1	2	3	4	5	6	7	8	9	10	total	Correct ratio
Total	29	Correct at first time	20	18	16	16	17	13	14	6	11	13	144	60.00%
Absent	5	Correct at second time	3	3	3	2	2	6	0	11	6	7	43	17.92%
		Third and above	1	3	5	6	5	5	10	7	7	4	53	22.08%



Figure 9 : Outcomes of the 5<sup>th</sup> in Exp group

Control g	group	Question No.	1	2	3	4	5	6	7	8	9	10	total	Correct ratio
Total	29	Correct at first time	18	20	17	13	13	15	10	14	11	15	146	60.83%
Absent	5	Correct at second time	4	2	4	7	4	4	4	5	7	3	44	18.33%
		Third and above	2	2	3	4	7	5	10	5	6	6	50	20.83%



Figure 10 : Outcomes of the 5<sup>th</sup> in Control group

- (1) There is no big difference between two groups.
- (2) It seems evident that students in both groups generally spend longer time to take this test.

The sixth E-test	:
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Exp gro	oup	Question No.	1	2	3	4	5	6	7	8	9	10	total	Correct ratio
Total	29	Correct at first time	20	18	10	18	21	16	11	8	21	20	163	65.20%
Absent	4	Correct at second time	3	1	9	3	3	2	8	7	1	3	40	16.00%
		Third and above	2	6	6	4	1	7	6	10	3	2	47	18.80%



Figure 11 : Outcomes of the 6<sup>th</sup> in Exp group

Control group		Question No.	1	2	3	4	5	6	7	8	9	10	total	Correct ratio
Total	29	Correct at first time	16	22	16	22	16	22	8	13	20	16	171	58.97%
Absent	0	Correct at second time	8	2	8	4	9	2	6	6	3	9	57	19.66%
		Third and above	5	5	5	3	4	5	15	10	6	4	62	21.38%



Figure 12: Outcomes of the 6<sup>th</sup> in Control group

- (1) At the first try, students in the Exp group perform a bit better than the students in the Control group do.
- (2) At the second try, students in the Control group perform a bit better than the students in the Exp group do.
- (3) Obviously, students in Control group generally spend longer time to take this test.

The sev	The seventh E-test :													
Exp gro	oup	Question No.	1	2	3	4	5	6	7	8	9	10	total	Correct ratio
Total	29	Correct at first time	24	16	22	18	17	18	15	18	21	26	195	72.49%
Absent	2	Correct at second time	2	3	2	5	5	4	4	4	4	1	34	12.64%
		Third and above	1	8	3	4	5	5	7	5	2	0	40	14.87%



Figure 13: Outcomes of the 7th in Exp group

Control group		Question No.	1	2	3	4	5	6	7	8	9	10	total	Correct ratio
Total	29	Correct at first time	24	17	16	16	16	21	18	18	21	22	189	70.00%
Absent	2	Correct at second time	2	5	3	7	8	3	2	6	2	3	41	15.19%
		Third and above	1	5	8	4	3	3	7	3	4	2	40	14.81%



Figure 14: Outcomes of the 7<sup>th</sup> in Control group

- (1) At the first try, students in Exp group perform a bit better than students in Control group do. Conversely at the second try.
- (2) Generally, outcomes between two groups look very close.

The eighth E-test :	The	eighth	E-test:
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Exp gro	oup	Question No.	1	2	3	4	5	6	7	8	9	10	total	Correct ratio
Total	29	Correct at first time	22	21	22	13	19	19	5	3	-	-	124	84.35%
Absent	6	Correct at second time	1	2	1	5	4	1	0	0	١	-	14	9.52%
		Third and above	0	0	0	5	0	3	0	1	1	-	9	6.12%



Figure 15: Outcomes of the 8<sup>th</sup> in Exp group

Control g	group	Question No.	1	2	3	4	5	6	7	8	9	10	total	Correct ratio
Total	29	Correct at first time	24	22	18	13	17	15	1	3	-	١	113	71.97%
Absent	5	Correct at second time	0	1	4	5	3	4	0	0	-	-	17	10.83%
		Third and above	0	1	2	6	4	5	9	0	-	-	27	17.20%



Figure 16: Outcomes of the 8th in Control group

- (1) This E-test only contains eight items because each has more computation involved.
- (2) Students in experimental group perform clearly better than students in control group do.
- (3) Close examination on the performances of Exp group indicates that they really make progress in E-test.

## Conclusion

Note that this study basically covers the content of calculus (II). We know that the road to learn calculus is not always straight and smooth, and successful learning usually requires appropriate pressure and self-regulation, as well as stamina and patience. We believe that "It is sometimes tough, but learners stick with it necessarily." Based on analyses of collected data, we did find that most students agreed these approaches to help their learning. Comparing with calculus (I) last semester, the results from interviews indicated that students were less anxious about calculus (II) in midterm or final comprehensive tests. In general, more students in experiment group have a higher self-learning motivation, a high percentage of students rated this course as more than interesting and dynamic organization, and more students use video materials for reviews after class. Indeed, almost all students perform calculus (II) better than calculus (I).

Although students in control group perform E-test a bit better than the students in experimental group do in several times. However, students in experimental group increase 11.5% from midterm to final comprehensive test, and students in control group only increase 7.9%. Much more, among 6 (in the experimental group) of 7 students (in the whole class) overwhelmingly increase their scores (more than 20 points) from midterm to final comprehensive test. Thus, our approaches obviously arouse the interest of students.

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# Appendix: (E-test 4)

1. Evaluate the definite integral.  $\int_{\ln 2}^{\ln 4} e^{-x} dx = ?$ 

(A) 6 (B)  $\frac{1}{16}$ (C)  $\frac{3}{4}$ (D)  $\frac{1}{4}$ (E) No answer

Hint: (A)(B)(C)(E): Note the derivative:  $D(e^{-x}) = -e^{-x}$  and recall the identity:  $e^{\ln X} = X \; .$ 

2. Differentiate the function  $f(x) = \ln\left(\frac{e^{5x}+1}{e^{2x}+1}\right)$ .

(A) 
$$\frac{2e^{2x} + 1}{5e^{2x} + 1}$$
  
(B) 
$$\frac{5e^{5x}}{e^{5x} + 1} - \frac{2e^{2x}}{e^{2x} + 1}$$
  
(C) 
$$\frac{5e^{5x}}{e^{5x} + 1} + \frac{2e^{2x}}{e^{2x} + 1}$$
  
(D) 
$$\frac{e^{2x} + 1}{e^{5x} + 1}$$
  
(E) 
$$\frac{e^{5x}}{e^{5x} + 1} - \frac{e^{2x}}{e^{2x} + 1}$$

Hint: (A)(C)(D)(E): Use the property  $\ln(\frac{A}{B}) = \ln A - \ln B$  first, then differentiate

both sides ..

3. Find the indefinite integral.  $\int 6^{5x} dx = ?$ 

(A) 
$$\frac{1}{\ln 6} 6^{5x} + C$$
  
(B)  $\frac{1}{5} 6^{5x} + C$   
(C)  $\frac{\ln 6}{5} 6^{5x} + C$   
(D)  $\frac{1}{5\ln 6} 6^{5x} + C$   
(E)  $5(\ln 6) 6^{5x} + C$ 

Hint: (A)(B)(C)(E): Recall  $D(6^{5x}) = ?$ 

4. Find an equation of the tangent line to the graph of  $y = \log_2 x$  at the point (32,5).

(A) 
$$y = 5 + \frac{1}{\ln 2}(x - 32)$$

(B) 
$$y=5+\frac{1}{2\ln 32}(x-32)$$
  
(C)  $y=5+\frac{1}{32\ln 2}(x-32)$   
(D)  $y=5-\frac{1}{\ln 2}(x-32)$   
(E)  $y=5+\frac{1}{32}(x-32)$ 

Hint: (A)(B)(D)(E): Recall  $D(\log_2 x) = ?$  Note that slope of tangent line is y'(32).

5. Write the following expression in algebraic form. sin(arccos(2x)) = ?

(A).  $\sqrt{1-4x^2}$ (B).  $1-2x^2$ (C).  $1+2x^2$ (D).  $1+4x^2$ (E).  $\sqrt{1-2x^2}$ 

Hint: (B)(C)(D)(E) : Recall that if  $\theta = \arccos(2x)$ , then  $\cos \theta = 2x$ 

6. Find the integral  $\int \frac{t}{t^4 + 81} dt = ?$ 

(A) 
$$\frac{1}{18} \arctan 9t^2 dt + C$$
  
(B)  $\frac{1}{18} \arctan \frac{t^2}{9} dt + C$ 

(C) 
$$\arctan \frac{1}{81} dt + C$$

(D) 
$$\frac{1}{9} \arctan 81t^2 dt + C$$

(E) 
$$\arctan\frac{t}{9}dt + C$$

Hint:

(A)(C)(D)(E): Recall 
$$\int \frac{du}{a^2 + u^2} = ?$$

7. Find the area of the shaded region for the function  $y = \frac{5}{\sqrt{4-x^2}}$ .



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(B) 
$$\frac{5\pi}{6}$$
  
(C)  $\frac{\pi}{2}$   
(D)  $\frac{2\pi}{3}$   
(E)  $\frac{\pi}{3}$ 

Hint: (A)(C)(D)(E) : Recall  $\int \frac{du}{\sqrt{a^2 - u^2}} = ?$ 

8. Find the indefinite integral.  $\int \sinh(6-3x)dx = ?$ 

(A) 
$$\frac{1}{6}\operatorname{sech}(6-3x) + C$$
  
(B)  $\frac{1}{3}\operatorname{sech}(6-3x) + C$   
(C)  $\frac{1}{6}\cosh(6-3x) + C$   
(D)  $\frac{-1}{3}\cosh(6-3x) + C$   
(E)  $\frac{1}{3}\cosh(6-3x) + C$ 

Hint: (A)(B)(C)(E): Recall  $D[\sinh U] = ? D[\cosh U] = ?$ 

9. Find the derivative of the function  $y = \cosh^{-1}(5x)$ 

(A) 
$$y' = \frac{5}{1-25x^2}$$
  
(B)  $y' = -\frac{5}{25x^2+1}$   
(C)  $y' = \frac{5}{\sqrt{25x^2-1}}$   
(D)  $y' = \frac{5}{\sqrt{25x^2+1}}$   
(E)  $y' = \frac{5}{\sqrt{1-25x^2}}$ 

Hint: (A)(B)(D)(E): Note how to differentiate inverse hyperbolic functions,  $D[\cosh^{-1} u] = ?$ 

10. Evaluate the definite integral.  $\int_{1}^{7} \frac{e^{7\sqrt{x}}}{\sqrt{x}} dx = ?$ 

(A)  $e^{7\sqrt{7}} - e^{7}$ (B)  $\frac{e^{7\sqrt{7}} - e^{7}}{7}$ (C)  $\frac{2(e^{7\sqrt{7}} - e^{7})}{3(7)^{3/2}}$ 

(D) 
$$\frac{e^{7\sqrt{7}} - e^{7}}{14}$$
  
(E)  $\frac{2(e^{7\sqrt{7}} - e^{7})}{7}$ 

Hint: (A)(B)(C)(D): Evaluate the definite integral of an exponential function using substitution. Note that  $D[e^u] = ?$