# Designing a Classification Toolkit for Mathematically-Deficient $4^{\text {th }}$ Grade Students: A Case Study in Vietnam 

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#### Abstract

The theory of educating slow-learning students has pointed out that, the first and most important step in this study is to identify and categorize the slow learners. In order for this study to be carried out effectively, a feasible and scientific procedure which complies the teachers' ability with educational environment in different schools is highly required (Brennan, W. Kyran (1974)), (Reddy and Ramar (2006)), (Vu, Q. Chung, Dao, T. Lai, Do, T. Dat, Tran, N. Lan, Nguyen, Q. Hung and Le, N. Son (2005)). The following study will examine some studies of categorizing slow-learning students, as well as suggesting a method of categorizing $4^{\text {th }}$-grade students who perform poorly in mathematics via the assessing mathematical ability toolkit. To develop the assessing mathematical ability toolkit to categorize slow-learning $4^{\text {th }}$ grade students, we have focused on some of the following tasks: (i) Determining the criteria for creating sets of exercises, (ii) Assessing the reliability and validity of the toolkit, and (iii) Choosing the conditions for categorizing slow-learning students.


Keywords: categorizing, slow-learning students, mathematics, $4^{\text {th }}$ grade.

## 1. Introduction

There are various methods of categorizing slow-learning students: Budanui, A. A (1960) believes that low performance in students is conventional in specific circumstances so he divided slow-learning into two types: Absolute slow-
learning and relative slow-learning. Inkovlev, N. M (1962) and other Polish educationists share the same notion. They believe this phenomenon is demonstrated in two different ways: Evidently and potentially. In terms of internal and external factors that motivate the students, Kalnukova, Z (1962), I divided slow-learning students into two groups: those who are academically abandoned and those who are academically deficient. In terms of the duration, extent and level of low performance, Genmont, A. M (1959) suggested 3 groups of underachievers: (1) Completely and seriously deficient in every subject over a long period, (2) Relatively and stably deficient in parts of the curriculum of some complex subjects (Mathematics, Foreign Languages), (3) Temporarily deficient in a random subject, but can be easily resolved (МЕНЧИНСКАЯ Н. А. КАЛМЬLКОВАЗ. И. (1964)).
In terms of personality structure, there is another categorization. Some scientists such as Babanskij, Iu. K (1964); Menchinskaja, N. A (1964), Kazanskij, N. G (1964) (МЕНЧИНСКАЯ Н. А. КАЛМЬЦКОВАЗ. И. (1964)) divided slowlearners based on the premise of combining two basic personality complexes: the first complex is characterized by features of logical thinking (relating to academic levels), the second one is characterized by personal trends including learning attitude and internal point of view. Thus, there are 3 different 2combinations between the aforementioned complexes and 3 groups of slowlearning students: (1) Poor logical thinking coupled with positive learning attitude and strong point of view, (2) Good logical thinking coupled with negative learning attitude and partial or no point of view, (3) Poor logical thinking coupled with partial to or point of view.
In terms of the students' cognitive ability, World Health Organization (WHO) divides slow-learners into 3 groups based on their IQ scores: (1) The educable mentally retarded (EMR) who have IQ ranging from 50-80, (2) the trainable mentally retarded (TMR) who have IQ ranging from $20-50$, (3) the severely and profoundly handicapped (SPH) who have IQ ranging from 8-20 (Brennan, W. K. (1974)), (Curtis, K., \& Shaver, J.P. (1980)).

In terms of the mechanism for slow development in functional areas of the brain, Tran, T. T, based on results from Luria 90 test, clinical evaluations, electroencephalogram (EEG) diagnoses, has suggested 3 groups: (1) Slow development in the Frontal, Parietal and Temporal lobes in both cerebral hemispheres, (2) slow development in the Occipital lobes in both cerebral hemispheres, (3) slow development in the left Temporal lobe (Tran, T. T. (1997)). Based on indications of cognitive limitations, psychologists have suggested the following categories: (1) Those who have poor memory, (2) those who have attention deficit disorder, (3) those who have intellectual disabilities, (4) those who have linguistic disabilities. For mathematically-deficient students in primary school, we can categorize them on the basis of the curriculum contents: slow learners in arithmetic, slow learners in geometry, slow learners in problemsolving, slow learners in statistics. In terms of levels of knowledge acquisition (Reddy and Ramar (2006)),there are: (1) slow learners who are lacking mathematical concepts or unable to memorize the principles, theorems or formulae, (2) slow learners who do not understand or remember the nature of the problems, (3) slow learners who are unable to apply mathematical knowledge to solving problems (Vu, Q. C., Dao, T. L., Do, T. D., Tran, N. L,

Nguyen, H. Q., \& Le, N. S. (2005)).
Therefore, categorizing slow-learners is crucial and has been an interesting subject of study for many authors. These studies, however, only approached this matter from diagnostic, neuropsychological and educational-psychological aspects. With these categorizations, teachers will come up against a great many difficulties in identifying slow learners via traditional methods. In reality, in order to effectively help low-performing students, teachers need a categorizing toolkit in the form of exercise sets so as to understand the students' level of mathematical knowledge acquisition, they can pinpoint the students' difficulties, mistakes and gaps in knowledge (Nguyen, V. C., Le, T. N., \& Phan, T. Q., (2002)). Those are the points on which we have focused and aimed to resolve in our research. In order to develop such a toolkit, we have carried out the following tasks: (i) Determining the criteria for creating sets of exercises, (ii) Assessing the reliability and validity of the toolkit, and (iii) Choosing the conditions for categorizing slow-learning students. Here we have chosen $4^{\text {th }}$ grade students to be our research subjects and the aim of this toolkit is to categorize mathematically-deficient $4^{\text {th }}$ grade students. The statistics used in this research are from some primary schools in Thai Nguyen and Phu Tho provinces in Vietnam.

## 2. Content

### 2.1. The criteria for developing the toolkit

Based on the mandatory standards of $4^{\text {th }}$ grade mathematics and the minimum standards of elementary mathematics (Do, D. H., Do, T. D., Dao, T. L., \& Do, T. H (2015)), we have built an assessing toolkit in the form of an exercise system aiming to test math proficiency of $4^{\text {thg }}$ grade students, through which we can identify and categorize mathematically-deficient $4^{\text {th }}$ grade students. In order to meet the requirements for elementary mathematics in general, the students must fully understand the following areas and these can also be regarded as the criteria for evaluating math proficiency of $4^{\text {th }}$ grade students:
1- Recognizing and understanding the meaning of numbers: Capable of counting, analyzing the formation and comparing between different numbers
2- Arranging the arithmetic algorithm and calculating: Capable of computing four basic arithmetic operations
3- Geometry: Capable of identifying basic shapes, properties of shapes. Know the formulae for calculating the circumference, diameter and area of shapes
4- Units of measurement: Understand and memorize units of measurement table, capable of converting between metric units
5- Problem solving: Capable of solving practical mathematical problems
Therefore, the exercise system must consist of all 5 above-mentioned areas. Meanwhile, in each area, the system must be able to assess which stage in the development process the contemporary knowledge of the student is at. In other words, which grade is the student's understanding of each mathematical area equivalent to? The system should be also able to identify which problems and shortcomings the children are experiencing in each mathematical area.

### 2.2. Introduction of the toolkit

From the listed criteria and skill requirements in each mathematical area from $1^{\text {st }}$ grade to $4^{\text {th }}$ grade, we have constructed a toolkit assessing math proficiency of $4^{\text {th }}$ grade students in which the 5 listed areas correspond to 5 domains. In each
domain, the exercises are designed in chronological order starting from the beginning of the knowledge acquisition process up to the contemporary period ( $4^{\text {th }}$ grade). The level of the exercises the students manage to complete will reflect their level of knowledge acquisition in terms of scores.
Content 1: Assessing the ability to recognize numbers and the meaning of numbers
Type 1: Read and write numbers: two-digit numbers (1st grade); three-digit numbers ( $2^{\text {nd }}$ grade); five-digit numbers ( $3^{\text {rd }}$ grade); seven-digit numbers ( $4^{\text {th }}$ grade).
Type 2: Compare and arrange numbers: Find the largest number in a sequence of 3digit numbers ( $2^{\text {nd }}$ grade); Continue a sequence of 5 -digit numbers ( $3^{\text {rd }}$ grade); Identify fractions which are larger than 1 ( $4^{\text {th }}$ grade).
The exercise system corresponding "Content 1 " is called "Scale A", which is suggested as below:
A. UNDERSTANDING NUMBERS AND MEANING OF NUMERS

A1. READ AND WRITE NUMBERS

| No. | Numericals | Written number | Correct (V) |
| :---: | :---: | :---: | :---: |
|  | 10356217 | Ten million three hundred and fifty-six thousand two hundred and seventeen |  |
| 1 |  | Twenty million four hundred and sixty-three thousand two hundred and six | $1 p t$ |
| 2 | 67246 | ......................................... | $1 p t$ |
| 3 | ...... | One million two hundred and thirty-four | $1 p t$ |
| 4 | 222 | ................................................. | $1 p t$ |
| 5 | .............. | Ninety nine | $1 p t$ |
| 6 | $\frac{5}{7}$ |  | $1 p t$ |
| 7 | ............... | Eighteen twenty-fifths | $1 p t$ |

Total A1: ...../7 points
A2. COMPARING AND ARRANGING NUMBERS

| No. | Exercise | Correct ( |
| :---: | :---: | :---: |
| 8 | Find the largest number among 395; 695; 375 | 1pt |
| 9 | Fill in the blanks: 18 301;18 302; ................; ................; ......................... 18 306; ............; | 1pt |
| 10 | Circle the fractions which are larger than 1: $\frac{5}{7}$ $\frac{3}{2}$ $\frac{12}{2}$ $\frac{13}{11}$ <br> $-;$ $\ldots$,    | 1 pt |

Total A2:....../3 points
Total Scale A= A1+A2: ......./10 points
Common mistakes:

## Content 2: Assessing the ability to arrange the arithmetic algorithm and calculate

Type 1: Addition: No-carrying addition (1st grade); one-carrying addition (2 ${ }^{\text {nd }}$ grade); 2-carrying addition (3 ${ }^{\text {rd }}$ grade); more-than-2-carrying addition, adding fractions with the same and different denominator ( $4^{\text {th }}$ grade)
Type 2: Subtraction: No-carrying subtraction (1st grade); one-carrying subtraction (2 ${ }^{\text {nd }}$ grade); 2-carrying subtraction (3rd grade); more-than-2-carrying subtraction, subtracting fractions with the same and different denominator (44 grade)
Type 3: Multiplication: Multiplication table (2 $2^{\text {nd }}$ grade); one-digit multiplication ( $2^{\text {nd }}$ and $3^{\text {rd }}$ grade); 2-digit and 3-digit multiplication, fraction multiplication (3rd and $4^{\text {th }}$ grade)
Type 4: Division: Division table (2 ${ }^{\text {nd }}$ grade); one-digit division (2 $2^{\text {nd }}$ and $3^{\text {rd }}$ grade); 2 -digit and 3 -digit division, fraction division ( $3^{\text {rd }}$ and $4^{\text {th }}$ grade)
The exercise system corresponding to "Content 2" is called "Scale B", which is suggested as below:
B. USING THE ARITHMETIC ALGORITHMS TO CALCULATE

B1. ADDTION SKILL

| No. | Exercises |  | Correct (V) |
| :---: | :---: | :---: | :---: |
|  | Calculate | Answer |  |
| 11 | $23+14$ |  | 1pt |
| 12 | $239+517$ |  | 1pt |
| 13 | $356+276$ |  | 1pt |
| 14 | 47865 + 78537 |  | 2pts |
| 15 | $\frac{3}{5}+\frac{2}{5}$ |  | 1pt |
| 16 | $\frac{5}{4}+\frac{2}{3}$ |  | 1pt |

Total B1: ....../ 7 points
B2. SUBTRACTION SKILL

| No. | Exercises |  | Correct <br> (V) |
| :--- | :--- | :--- | :--- |
|  | Answer |  | 1 pt |
| 17 | $56-13$ |  | 1 pt |
| 18 | $451-23$ |  | 1 pt |
| 19 | $534-265$ |  | 2 pts |
| 20 | $123456-10678$ |  | 1 pt |
| 21 |  |  |  |


|  $\frac{5}{7}-\frac{2}{7}$   <br> 22 $\frac{5}{3}-\frac{2}{4}$  1 pt <br> Total B2: ....../7 points    |
| :--- |
| B3. MULTIPLICATION SKILL |


| No. | Calculate |  | Correct |
| :--- | :--- | :--- | :--- |
|  | Answer |  |  |
| 23 | $3 \times 6=$ <br> $4 \times 8=$ |  | 2 pts |
| 24 | $12 \times 4=$ | 2 pts |  |
| 25 | $23 \times 12=$ |  | 2 pts |
| 26 | $1456 \times 123=$ | 2 pts |  |
| 27 | $\frac{5}{3} \times \frac{2}{7}$ |  | 2 pts |

Total B3: ....../ 10 points
B4. DIVISION SKILL

| No. | Exercises |  | Correct |
| :---: | :---: | :---: | :---: |
|  | Calculate | Answer |  |
| 28 | $\begin{aligned} & 6: 2= \\ & 8: 4= \end{aligned}$ |  | 2pts |
| 29 | $84: 4=$ |  | 2pts |
| 30 | $276: 12=$ |  | 2pts |
| 31 | 4428 : 123 |  | 2pts |
| 32 | $\frac{2}{3}: \frac{4}{5}$ |  | 2pts |

Total B4: ....../10 points
Total Scale B = B1+B2+B3+B4=........../34 points
Common mistakes: $\qquad$

## Content 3: Assessing geometry skills

Type 1: Match the shapes with the correct names and colors (1st grade)
Type 2: Calculate the diameter of a triangle (2 $2^{\text {nd }}$ grade)
Type 3: Calculate the area of a rectangle (3rd grade)
Type 4: Draw parallel and perpendicular lines, identify different types of angles (4th grade)
The exercise system corresponding to "Content 3 " is called "Scale C", which is suggested as below:

## C. GEOMETRY



Total: $\qquad$ / 12 points

Common mistakes: $\qquad$

## Content 4: Assessing understanding of units of measurement

Types of metric units: weight, time, length, area. In each type we will test understanding of the metric unit chart and unit conversion.

The exercise system corresponding "Content 4" is called "Scale D", which is suggested as below:

## D. UNITS OF MEASUREMENT

## D1. UNITS OF MASS

| No. | Exercises | Correct |
| :---: | :---: | :---: |
| 39 | 1 centitonne $=\ldots \ldots \ldots \ldots . . \mathrm{kg}$ | 1pt |
| 40 | 1 quintal = .............centitonne | 1pt |
| 41 | 1 quintal $=\ldots \ldots \ldots \ldots \ldots \ldots . \mathrm{kg}$ | 1pt |
| 42 | 1 tonne $=\ldots \ldots \ldots \ldots \ldots .$. quintal | 1 pt |
| 43 | 1 tonne $=\ldots \ldots \ldots \ldots \ldots \ldots . \mathrm{kg}$ | 1 pt |
| 44 | 1 centitonne $7 \mathrm{~kg}=\ldots \ldots \ldots \ldots \ldots . . \mathrm{kg}$ | 2pts |
| 45 | 4 quintal $60 \mathrm{~kg}=\ldots \ldots \ldots \ldots \ldots \ldots . . \mathrm{kg}$ | 2pts |

Total D1: ........./9 points.

## D2. UNITS OF TIME

| No. | Exercises | Correct |
| :---: | :---: | :---: |
| 46 | 1 hour $=\ldots \ldots \ldots \ldots \ldots \ldots$. minutes | 1pt |
| 47 | 1 minute $=\ldots \ldots \ldots \ldots \ldots \ldots$. seconds | 1 pt |
| 48 | 1 century = ...............years | 1pt |
| 49 | 1 minute 8 seconds = ..............seconds | 2pts |
| 50 |  | 2 pts |

## D3. UNITS OF LENGTH

| No. | Exercises | Correct $(\mathbb{V})$ |
| :--- | :--- | :--- |
| 51 | $1 \mathrm{~km}=\ldots \ldots \ldots \ldots . \mathrm{m}$ | 1 pt |
| 52 | $1 \mathrm{~m}=\ldots \ldots \ldots \ldots \ldots \mathrm{dm}$ | 1 pt |
| 53 | $1 \mathrm{dm}=\ldots \ldots \ldots \ldots \ldots . \mathrm{cm}$ | 1 pt |
| 54 | $1 \mathrm{~cm}=\ldots \ldots . \mathrm{mm}$ | 1 pt |
| 55 | $1 \mathrm{~m}=\ldots \ldots \ldots . \mathrm{cm}$ | 1 pt |
| 56 | $1 \mathrm{~m}=\ldots \ldots \ldots \ldots \mathrm{mm}$ | 1 pt |
| 57 | $2 \mathrm{~km} 35 \mathrm{~m}=\ldots \ldots \ldots . \mathrm{m}$ | 2 pts |
| 58 | $3 \mathrm{~m} 2 \mathrm{~cm}=\ldots \ldots \ldots . . \mathrm{cm}$ | 2 pts |
|  |  |  |

Total D3: ........./10 points.

## D4. UNITS OF AREA

| No. | Exercises | Correct $(\mathbb{V})$ |
| :--- | :--- | :--- |
| 59 | $1 \mathrm{~m}^{2}=\ldots \ldots \ldots \ldots \ldots . \mathrm{dm}^{2}$ | 1 pt |
| 60 | $1 \mathrm{dm}^{2}=\ldots \ldots \ldots \ldots \ldots . \mathrm{cm}^{2}$ | 1 pt |
| 61 | $1 \mathrm{~m}^{2}=\ldots \ldots \ldots \ldots \ldots . \mathrm{cm}^{2}$ | 2 pts |
| 62 | $1 \mathrm{~km}^{2}=\ldots \ldots \ldots \ldots \ldots . \mathrm{m}^{2}$ | 2 pts |
| 63 | $10 \mathrm{dm}^{2} 2 \mathrm{~cm}^{2}=\ldots \ldots \ldots \ldots \ldots . . \mathrm{cm}^{2}$ | 2 pts |
| 64 | $9900 \mathrm{~cm}^{2}=\ldots \ldots \ldots . . \mathrm{dm}^{2}$ | 2 pts |

Total D4: ........./10 points.
Total Scale D= D1+D2+D3+D4 = $\qquad$ . 36 points

Common mistakes: $\qquad$

## Content 5: Assessing the ability to solve practical problems

Type 1: 1-operation problems about addition (1st grade)
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## Type 2: 1-operation problems about more than/less than (2nd grade)

Type 3: 2-operation problems (3rd grade)
Type 4: 2-to-3-operation problems (4th grade)
The exercise system corresponding to "Content 5 " is called "Scale E", which is suggested as below:

## E. PROBLEM SOLVING

| No. | Exercises |  | Correct (V) |
| :---: | :---: | :---: | :---: |
|  | Problem | Answer |  |
| 65 | Exercise 1: Minh has 12 pieces of candy; Mai has 23 pieces of candy. How many pieces of candy do Minh and Mai have? | ...................................... | 2pts |
| 66 | Exercise 2: The small jar holds 10 litters of fish sauce; the big jar holds 5 litters more than the small jar. How many litters of fish sauce does the big jar hold? |  | 2pts |
| 67 | Exercise 3: 42 identical cups are placed into 7 boxes. If there are 4572 cups, how many boxes are they placed into? |  | 2pts |
| 68 | Exercise 4: There are 45 students in a class, $\frac{3}{4}$ of whom are girls. How many boys and girls are there in the class? | $\square$ | 2pts |

Total: $\qquad$ 8 points
Common mistakes:

### 2.3. Evaluating the reliability and validity of the toolkit

After being designed, constructed, and consulted by professionals, the toolkit has been completed, comprised of a system of 68 exercises with 5 domains. The points are given in accordance with the scale of each domain with the total sum of 100 . We have conducted a small-scale test to determine the reliability and
validity of the scales before conducting a large-scale test. To test the reliability of the toolkit, we have applied the Test-Retest Method to twenty $4^{\text {th }}$ grade students from Tu Xa 2 elementary school in late April, 2015. The students' results from the two tests at a one-week interval have been summed up in the following table:

Table 1: The results of 20 students in two tests

| Student <br> (i) | First test score $x_{i 1}$ | Second test score <br> $x_{i 2}$ | Deviation | Mean | Variance |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 84 | 92 | -8 | 88 | 32 |
| 2 | 100 | 100 | 0 | 100 | 0 |
| 3 | 88 | 80 | 8 | 84 | 32 |
| 4 | 56 | 62 | -6 | 59 | 18 |
| 5 | 72 | 76 | -4 | 74 | 8 |
| 6 | 30 | 28 | 2 | 29 | 2 |
| 7 | 86 | 80 | 6 | 83 | 18 |
| 8 | 68 | 74 | -6 | 71 | 18 |
| 9 | 88 | 80 | 8 | 84 | 32 |
| 10 | 100 | 98 | 2 | 99 | 2 |
| 11 | 90 | 98 | -8 | 94 | 32 |
| 12 | 86 | 82 | 4 | 84 | 8 |
| 13 | 48 | 46 | 2 | 47 | 2 |
| 14 | 74 | 76 | -2 | 75 | 2 |
| 15 | 72 | 70 | 2 | 71 | 2 |
| 16 | 86 | 88 | -2 | 87 | 2 |
| 17 | 54 | 48 | 6 | 51 | 18 |
| 18 | 100 | 88 | 12 | 94 | 72 |


| 19 | 56 | 64 | -8 | 60 | 32 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 20 | 46 | 42 | 4 | 44 | 8 |
| Mean | 74.2 | 73.6 | $\bar{x}_{i}=\mathbf{0 . 6}$ | $\bar{x}=\mathbf{7 3 . 9}$ |  |

The coefficient of reliability of the toolkit can be calculated using the following formula
$R=\frac{S_{T}^{2}}{S_{T}^{2}+S_{E}^{2}}$ in which: $R$ is the coefficient of reliability
$S_{E}^{2}$ is the deviation in the test scores $S_{E}^{2}=\frac{S_{1}^{2}+S_{2}^{2}+\ldots+S_{N}^{2}}{N}, S_{i}^{2}$ being the variance of student $i, N$ being the number of participants.
$S_{T}^{2}$ is the actual score reflecting the student's ability. $S_{T}^{2}=\frac{B M S-W M S}{k}$ (with $B M S=\frac{1}{N-1} \sum_{i=1}^{N} 2\left(\overline{x_{i}}-\bar{x}\right)^{2}$ and $W M S=\frac{1}{N} \sum_{i=1}^{N} S_{i}^{2}, \overline{x_{i}}$ being the mean score of student i in the two tests; $\bar{x}$ being the mean of the test scores; $k$ being the number of tests conducted on one student, in this case $k=2$ ). The results are $S_{T}^{2}=354.1 ; S_{E}^{2}=17$, and the coefficient of reliability of the toolkit is $R=0.95$.
These results show that the stability of the classification toolkit for mathematically-deficient $4^{\text {th }}$ grade students is rather high. (Nguyen, V. T (2015)). The validity of the toolkit has been taken into account with two values: internal validity and external validity. The internal validity answers the question: Is the toolkit well-structured? Does it conform to the whole scale? This index is assessed using the coefficient of correlation between different domains, as well as between the domains and the whole scale. The toolkit will have a high internal validity (construct validity) if the smaller scales match up with one another and with the whole scale. The following table illustrates the correlation between the 5 domains, using figures from the test results of the abovementioned 20 students in the first test:

Table 2: Coefficient of correlation between domains

| Coefficient of <br> correlation | Domain <br> $\mathbf{A}$ | Domain <br> B | Domain <br> $\mathbf{C}$ | Domain <br> $\mathbf{D}$ | Domain <br> $\mathbf{E}$ | The whole <br> scale |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Domain A |  | 0.933 | 0.788 | 0.814 | 0.780 | 0.912 |
| Domain B |  |  | 0.886 | 0.887 | 0.854 | 0.982 |
| Domain C |  |  |  | 0.791 | 0.762 | 0.905 |
| Domain D |  |  |  |  | 0.814 | 0.948 |
| Domain E |  |  |  |  |  | 0.882 |
| The whole scale |  |  |  |  |  |  |

The table shows that the coefficient of correlation between each domain and the coefficient of correlation between the domains and the whole scale both have positive value (from 0.762 to 0.982 ), which means that there is a direct correlation between them. On the other hand, these figures reflect the structural unity of elementary math in Vietnam.

## 3. Experimenting the classification toolkit for mathematically-deficient $4^{\text {th }}$ grade students

Having confirmed the reliability and validity of the toolkit, we conducted an experiment to identify and classify slow-learning students in 156 students from three schools: Tu Xa 2 Elementary school ( 65 students), Cao Mai Elementary school ( 56 students) and Linh Thong Elementary school ( 36 students). These schools are located in two provinces, Thai Nguyen and Phu Tho, Vietnam. The results are depicted in the following table, using SPSS program

Table 3: Collected figures

| N | Valid | 156 |
| :--- | :--- | ---: |
|  | Missing | 0 |
| Mean | 82.29 |  |
| Median | 86.00 |  |
| Mode | 88 |  |
| Std. Deviation | 14.562 |  |
| Minimum | 24 |  |
| Maximum | 100 |  |

Table 4: Frequency of test scores

| Valid | Frequency | Percent | Valid | Frequency | Percent |
| :--- | :--- | :--- | :--- | :--- | :--- |
| $\mathbf{2 8}$ | 1 | $0.6 \%$ | $\mathbf{8 1}$ | 1 | $0.6 \%$ |
| $\mathbf{2 9}$ | 1 | $0.6 \%$ | $\mathbf{8 2}$ | 7 | $4.5 \%$ |
| $\mathbf{3 0}$ | 1 | $0.6 \%$ | $\mathbf{8 3}$ | 5 | $3.2 \%$ |
| $\mathbf{3 1}$ | 1 | $0.6 \%$ | $\mathbf{8 4}$ | 10 | $6.4 \%$ |
| $\mathbf{3 2}$ | 2 | $1.3 \%$ | $\mathbf{8 5}$ | 10 | $6.4 \%$ |
| $\mathbf{4 6}$ | 1 | $0.6 \%$ | $\mathbf{8 6}$ | 6 | $3.8 \%$ |
| $\mathbf{5 7}$ | 1 | $0.6 \%$ | $\mathbf{8 7}$ | 10 | $6.4 \%$ |
| $\mathbf{5 8}$ | 2 | $1.3 \%$ | $\mathbf{8 8}$ | 12 | $7.7 \%$ |
| $\mathbf{6 0}$ | 2 | $1.3 \%$ | $\mathbf{8 9}$ | 7 | $4.5 \%$ |
| $\mathbf{6 1}$ | 2 | $1.3 \%$ | $\mathbf{9 0}$ | 6 | $3.8 \%$ |
| $\mathbf{6 2}$ | 1 | $0.6 \%$ | $\mathbf{9 1}$ | 3 | $1.9 \%$ |
| $\mathbf{6 3}$ | 2 | $1.3 \%$ | $\mathbf{9 2}$ | 7 | $4.5 \%$ |
| $\mathbf{6 4}$ | 3 | $1.9 \%$ | $\mathbf{9 3}$ | 4 | $2.6 \%$ |
| $\mathbf{7 2}$ | 1 | $0.6 \%$ | $\mathbf{9 4}$ | 9 | $5.8 \%$ |
| $\mathbf{7 4}$ | 1 | $0.6 \%$ | $\mathbf{9 5}$ | 4 | $2.6 \%$ |
| $\mathbf{7 5}$ | 1 | $0.6 \%$ | $\mathbf{9 6}$ | 3 | $1.9 \%$ |
| $\mathbf{7 6}$ | 7 | $4.5 \%$ | $\mathbf{9 7}$ | 2 | $1.3 \%$ |
| $\mathbf{7 7}$ | 2 | $1.3 \%$ | $\mathbf{9 8}$ | 2 | $1.3 \%$ |


| Valid | Frequency | Percent | Valid | Frequency | Percent |
| :--- | :--- | :--- | :--- | :--- | :--- |
| $\mathbf{7 8}$ | 8 | $5.1 \%$ | $\mathbf{9 9}$ | 2 | $1.3 \%$ |
| $\mathbf{7 9}$ | 4 | $2.6 \%$ | $\mathbf{1 0 0}$ | 2 | $1.3 \%$ |

Based on the above table, we have the following graph of distribution of the students' scores:

Graph 1: Distribution of $4^{\text {th }}$ grade students' test scores


The table has reflected the expected characteristics of the toolkit. The overall mean score of the students is over 82.29 out of a maximum of 100 . This can be explained by the expectation that this toolkit is designed to identify students who perform poorly in $4^{\text {th }}$ grade math, with the minimum requirements, so that at least $80 \%$ (the calculated figure is $81.8 \%$ ) of the students can complete most of the exercises. Moreover, the arithmetic domain including: number formation and operation already accounts for $44 / 100$ points of the scale; the remaining smaller scales have a certain minimum difficulty to ensure that it is possible for any regular $4^{\text {th }}$ grade student in their second semester to solve them, and can only be a challenge for slow-learning students.
The table of the score distribution of $4^{\text {th }}$ grade students - Graph 1 has fundamentally conformed to the rules of normal distribution - this is an essential element in identifying slow-learning students in $4^{\text {th }}$ grade. The results in Table 4 shows that the mean score of the students is $\mathrm{M}=82.29$ and the standard deviation is $\mathrm{SD}=14.56$. The specific results of the mean score and standard deviation of the domains are as follows:

Table 5: The mean score and standard deviation of each domain

| Domains | Total score | Domain <br> A | Domain B | Domain C | Domain $\mathbf{D}$ | Domain E |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| Mean score (M) | $\mathrm{M}_{\mathrm{s}}=82.29$ | $\mathrm{M}_{\mathrm{A}}=9.69$ | $\mathrm{M}_{\mathrm{B}}=29.29$ | $\mathrm{M}_{\mathrm{C}}=10.14$ | $\mathrm{M}_{\mathrm{D}}=26.47$ | $\mathrm{M}_{\mathrm{E}}=6.69$ |
| Standard <br> deviation (SD) | $\mathrm{SD}_{\mathrm{S}}=14.56$ | $\mathrm{SD}_{\mathrm{A}}=1.11$ | $\mathrm{SD}_{\mathrm{B}}=6.01$ | $\mathrm{SD}_{\mathrm{C}}=2.57$ | $\mathrm{SD}_{\mathrm{D}}=4.34$ | $\mathrm{SD}_{\mathrm{M}}=1.60$ |

Therefore, if the total test score of a student is T, we can divide the level of mathematical ability of $4^{\text {th }}$ grade students based on the distribution of the mean score $\mathrm{M}_{\mathrm{s}}$ and standard deviation $\mathrm{SD}_{\mathrm{s}}$ as follow:

Table 6: Categorization of $4^{\text {th }}$ grade students' mathematical ability

| Categories | Slow learners |  |  | Non-slow learners |  |
| :--- | :--- | :--- | :--- | :--- | :---: |
|  | Type 1: Non- <br> definite <br> knowledge in <br> all areas | Type 2: Non-definite <br> knowledge in some <br> areas | Basic knowledge of <br> mathematics, meeting <br> requirements in the <br> standard of 4th grade <br> math | Firm basis <br> in math |  |
|  | $T<M_{S}-2 S \mathrm{D}_{\mathrm{S}}$ | $M_{S}-2 \mathrm{SD}_{\mathrm{S}} \leq T<M_{S}-S \mathrm{D}_{\mathrm{s}}$ | $M_{s}-S \mathrm{D}_{\mathrm{s}} \leq T \leq M_{s}+S \mathrm{SI}$ | $T>M_{s}+S \mathrm{II}$ |  |
| Corresponding <br> score | $\mathrm{T}<53,17$ | $53,17 \leq T<67,73$ | $67,73 \leq T<96,85$ | $T \geq 96,85$ |  |

Based on the above categorization, Cao Mai elementary school does not have any type 1 slow-learning students. However, if we consider more criteria of domains $A$ and $B$, and call $T_{A}, T_{B}$ the total scores which students gained from domains A and B, with the same categorizing way as above, which means

Table 7: Categorizing slow learners according to three criteria

| Criteria |  | Slow learners Type 1 | Slow learners Type 2 |
| :--- | :--- | :---: | :---: |
| Total score of the <br> survey | Formula | $T<M_{S}-2 S \mathrm{D}_{\mathrm{S}}$ | $M_{S}-2 S \mathrm{D}_{\mathrm{S}} \leq T<M_{S}-S \mathrm{D}_{\mathrm{S}}$ |
|  | Correspondent <br> score | $\mathrm{T}<53,17$ | $53,17 \leq T<67,73$ |
| Score of domain A | Formula | $T_{A}<M_{A}-2 S \mathrm{D}_{\mathrm{A}}$ | $M_{A}-2 S \mathrm{D}_{\mathrm{A}} \leq T_{A}<M_{A}-S \mathrm{D}_{\mathrm{A}}$ |
|  | Correspondent | $\mathrm{T}_{\mathrm{A}}<7,47$ | $7,47 \leq T_{A}<8,58$ |


|  | score |  |  |
| :--- | :--- | :---: | :---: |
| Score of domain B | Formula | $T_{B}<M_{B}-2 S \mathrm{D}_{\mathrm{B}}$ | $M_{B}-2 S \mathrm{D}_{\mathrm{B}} \leq T_{B}<M_{B}-S \mathrm{D}_{\mathrm{B}}$ |
|  | Correspondent <br> score | $\mathrm{T}_{\mathrm{B}}<17,27$ | $17,27 \leq T_{B}<23,28$ |

So the rate of slow learners between schools is distributed as follows:

Table 8: Proportion of different student groups in chosen schools

|  |  |  |
| :---: | :---: | :---: |
|  | -Slow learners Type 1 aSlow learners Type 2 $\square$ Non-slow learners |  |
| Cao Mai primary school | Tu Xa 2 primary school | Linh Thong primary school |

And the rate (Slow learners Type 1: Slow learners Type 2: Non-slow learners) in the whole is $(4 \%: 8 \%: 88 \%)$. This result also corresponds to Newman's error analysis (1977) (Newman, M. A, (1977). Therefore, use the above system of exercises and consider domains using the three criteria: 1 . The total score of the survey, 2. Score of domain A, 3. Score of domain A with the determination according to the formula of Table 7, we can determine and categorize students bad at math in 4th grade Mathematics Subject in Vietnam more properly.

## Example:

The following table is the test results of a student (Ngo, D. Bang) from Tu Xa 2 elementary school - Lam Thao district - Phu Tho province. This student has the total test score $T=28 / 100$ points, Domain $A=4 / 10$ points, Domain $B=8 / 34$ points. According to the above criteria, this student is a Type 1 slow learner, whose common mistakes have been depicted as follow

Table 9: Analyzing the mistakes in a student's test

| Item |  | Maxi mum score | $\begin{gathered} \text { Resu } \\ \text { lt } \end{gathered}$ | Common mistakes |
| :---: | :---: | :---: | :---: | :---: |
| A. <br> Recognizing numbers and their meanings | A1 - Reading and writing numbers | 7 | 3 | Mistakes due to lack of knowledge of the composition of numbers with more than 3 digits |
|  | A2- Comparing and arranging numbers | 3 | 1 | Mistakes due to inability to compare fractions as well as multi-digit numbers |
| B. Using arithmetic algorithms to calculate | B1-Addition skills | 7 | 4 | Mistakes when adding multi-digit numbers with multiple carryings; not remembering the rule of adding fractions with unlike denominators |
|  | B2- Subtraction skills | 7 | 2 | Mistakes when subtracting with carryings; not remembering the rule of subtracting fractions with unlike denominators |
|  | B3- <br> Multiplication skills | 10 | 1 | Mistakes due to not remembering the multiplication table, not having any multiplication skill |
|  | B4- Division skills | 10 | 1 | Mistakes due to not remembering the division table, not having any division skill |
| C. Geometry |  | 12 | 4 | Mistakes due to not remembering the formula for area, the parallelism and perpendicularity of two straight lines, inability to differentiate basic types of angles. |
| D. Units of measurement | D1- Mass | 9 | 5 | Mistakes due to unfamiliarity to conversion of units of mass |
|  | D2- Time | 7 | 4 | Mistakes due to unfamiliarity to conversion of units of time |
|  | D3- Length | 10 | 1 | Mistakes due to unfamiliarity to conversion of units of length |


|  | D4- Area | $\mathbf{1 0}$ | $\mathbf{0}$ | Mistakes due to unfamiliarity to <br> conversion of units of area |
| :--- | :--- | :--- | :--- | :--- |
| E Problem solving | $\mathbf{8}$ | $\mathbf{2}$ | Mistakes right from the process of <br> analyzing, summarizing and <br> determining the problem lead to <br> inability to use the correct algorithm <br> and inability to give appropriate <br> answers |  |
| Total | $\mathbf{1 0 0}$ | $\mathbf{2 8}$ |  |  |

Assessment of the student's mathematical ability: Current mathematical ability is equal to that of a $1^{\text {st }}$ grade student. This student lacks the knowledge right from the understanding of numbers and basic calculations, resulting in consecutive difficulties in acquiring mathematical knowledge.
he solution to the case of student Ngo D. Bang: Math teacher had to tutor Ngo individually to fulfill the lacking knowledge in math for him, cut down general assignments in class, and give him individually suitable duties. Besides, the math teacher had more regular cooperation with the parents in instructing the students to review the lessons at home, as well as asked a group of better students to help him study math.

## 5. Conclusion

As mentioned in the introduction, there are many methods of identifying slow learners. However, not only does this method of using an exercise system categorize slow learners in terms of their cognitive abilities, but it can also identify the difficulties, mistakes and gaps in the students' knowledge. These are essential for a more effective orientation towards aiding slow learners.

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